

# Continuous Measurements and Quantitative Constraints - Challenge Problems for Discrete Modeling Techniques

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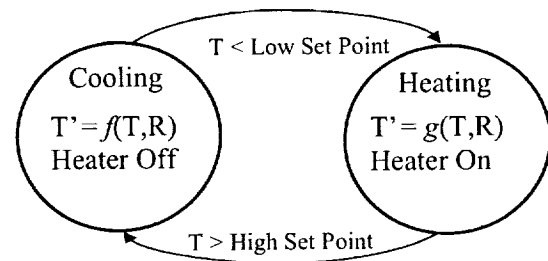
## Abstract

Many techniques in artificial intelligence operate on discrete models, wherein each variable of a system description may take on only a finite number of discrete values. These discrete models are easy to acquire, they have computational advantages, and there are many well-developed algorithms for manipulating them. In contrast, the world presents us with many continuous processes we would like to simulate, identify or control. Many discrete techniques from AI are regularly applied to discrete abstractions of continuous processes. This of course is not always possible. It's therefore important to consider whether one's continuous problem lends itself to being abstracted and solved as a discrete problem. We describe a set of modeling technique and algorithms for discrete, model-based diagnosis and control, in a manner we hope will be accessible to those outside the field. We then present a continuous problem in the domain of spacecraft state identification and control for which a discrete abstraction of the problem allows us to perform useful diagnosis and reconfiguration. We then present a seemingly similar problem for which developing a discrete abstraction was quite difficult and which did not result in as useful a diagnosis and control system. We contrast the two systems, and describe some of the problems that made the second problem far less suitable for use with a discrete model and discrete reasoning algorithms.

## 1 Introduction

Suppose we would like to create algorithms that perform computations about a physical system such as a spacecraft in order to perform tasks such as diagnosing its current condition, simulating its future operation, or planning a set of control inputs to move the system to a desired condition. In order to use such algorithms, we will require a model or formal description of the physical system. A *continuous model* includes real-valued attributes that may take on an infinite number of values and continuous functions

that compute the value of one attribute from another. Change is modeled as the derivative of one or more attributes over time. For example, a model of heating and cooling of a spacecraft might include continuous variables that represent the energy radiated from the spacecraft into space and the energy output of its heaters, and a set of differential equations that model thermal conductivity through the spacecraft's structure. When we begin to model complete systems, we may often find that the physical behavior of the system is continuous, but that a controller with discrete states controls it. A *hybrid model* includes both discrete states and continuous variables. A hybrid model can discretely transition from one state to another, and within each state can evolve continuously through a set of differential equations. Consider the following example.



**Figure 1 Simplified Continuous Thermostat**

Conceptually, Figure 1 illustrates a hybrid model of a simple thermostatic heating system. The variable  $T$  represents the current temperature of the system, while  $T'$  represents the derivative of the temperature with respect to time.  $R$  represents the thermal properties of the system being heated, for example its thermal conductance. When in the Cooling state, the controller turns the heater off, and the temperature falls according to some continuous function  $f$ . When the temperature falls below a low set point, the thermostat controller makes a discrete transition to the Heating state. In this state, the controller turns the

heater on, and the temperature rises according to some continuous function  $g$ . Such a model would help us to simulate the temperature of the system given the set points and the parameter  $R$ , would be useful in diagnosing whether the heater was operating properly, and so on.

While much of the world is hybrid, a significant amount of work in artificial intelligence concerns *discrete models*. In contrast to a continuous model, each attribute of a discrete model may take on only a finite number of discrete values. Thus, there is only a finite (though possibly very large) set of states the discrete model can attain. Using a discrete model has computational advantages, and a wide range of discrete modeling formalisms and algorithms have been developed or applied by the AI community. Examples of techniques that apply to discrete models include STRIPS-style planning and many of its extensions (see Boutilier, Dean & Hanks, 1995 for an overview), partially observable Markov decision processes (see Kaelbling, Littman & Cassandra), some of the work in model-based diagnosis (see Hamscher, Console & deKleer 1992 for an overview), and anything that makes use of a propositional logic encoding.

Fortunately, we can often capture the features of our hybrid system that are relevant to a particular task (e.g., planning, diagnosis, simulation or so on) in a discrete abstraction. That is, we can abstract an infinite number of hybrid behaviors into a finite number of discrete behaviors. For example, to determine whether or not the thermostat of Figure 1 is functioning correctly, it may be sufficient to create the discrete model illustrated in Figure 2. When the temperature level drops below a set point, the system enters the discrete heating state, wherein the heater must be on and the temperature must be rising. Any continuous behavior that fits this discrete description is normal behavior, and any that does not indicates a failure.

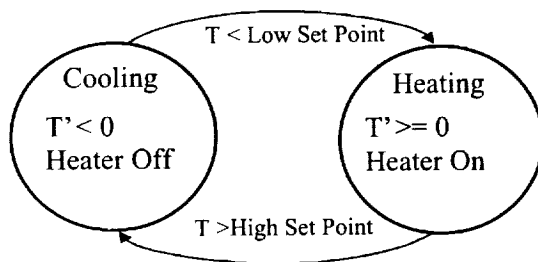


Figure 2 Qualitative Thermostat Model

If a discrete abstraction such as this provides sufficient information for the task at hand, then we may then apply our discrete techniques. Discrete abstractions are regularly applied in AI with great success. Examples of their use are too numerous to enumerate, but they include robot navigation (for example, Nourbakhsh, Powers & Birchfield, 1996), and spacecraft diagnosis and control (for example, Williams & Nayak, 1996).

The issue is then, when is a discrete abstraction sufficient, when is it insufficient, and how does one determine this before investing time writing a discrete model. We have spent the last few years applying discrete diagnosis and control systems to a variety of domains (Bernard, et al, 1998; Kurien, Nayak & Williams, 1998). In the following sections of the paper, we first describe a typical application to which we have applied discrete diagnosis and control techniques. We then give an intuition of how one particular discrete diagnosis and control system, called Livingstone (Williams & Nayak, 1996; Kurien & Nayak, 2000) operates and provide some intuitions on why it works well on the typical application. We then describe a domain that appears to be similar where discrete abstractions worked rather poorly. We then describe the types of problems that separate the two domains, and what capabilities a hybrid diagnosis and control system needs to have to address the more complex domain.

### 3 The Propulsion System Application

Figure 3 illustrates the redundant propulsion system used in the Cassini spacecraft, designed to last a seven year cruise to Saturn and autonomously insert itself into orbit around Saturn. The purpose of the system is to provide the appropriate amount of acceleration by combining fuel and an oxidizer in an engine for a specified amount of time. The helium tank is filled with helium under high pressure. Conceptually, controlling the system is straightforward. When the appropriate valves are opened, the high pressure in the helium tank pressurizes the oxidizer and fuel tanks. This forces oxygen and fuel into the engine where it is ignited to produce thrust. When sufficient thrust is achieved, the valves are closed.

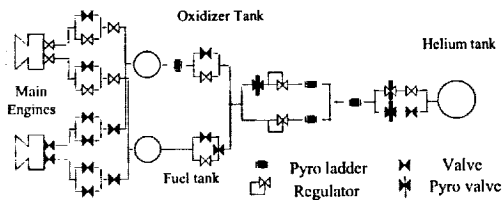


Figure 3- Engine Schematic

In actuality, the control problem is complicated by the redundancy needed to ensure success on a long mission. Two engines are provided in the case that one fails. Each engine is supplied with fuel and oxidizer through a complex arrangement of valves. Valves or pipe branches in parallel ensure that if valves stick closed, a redundant parallel valve can be used to allow fluid flow. Valves in series ensure that if valves stick open, an upstream valve can be closed to prevent fluid flow. Not shown are valve drivers that control the latch valves and a set of flow, pressure and acceleration sensors that provide partial observability of the system. There are approximately  $10^{15}$  possible configurations of the system including failures. Several hundred of those configurations produce thrust, depending upon which valves are open or closed. Given a set of failures, thrust configurations that can be reached without using a pyro valve are preferred, as pyro valves can only be opened or closed once. Regardless of the number of failures that occur, we'd like the control system to determine the current configuration of the propulsion system and find the best viable configuration of the system that will produce thrust.

Though this system is relatively complex, using only a discrete model we can answer the question of which valves are stuck open or closed and what actions should be taken to create a route for fuel and oxidizer to a working engine. The next section describes how this is accomplished.

## 2 Discrete Diagnosis & Control

Our discrete model of a hardware system must specify the components of the system (e.g. there are three tanks, twenty-eight valves, and assorted other parts). For each component, the model must specify the possible states, referred to as *modes*, the component may occupy (e.g. a valve may be open, closed, stuck open, or stuck closed). For each mode, the model must specify the component's behavior (e.g. a closed valve prevents flow). We must also specify the transitions. A transition moves the model from one mode to another when some condition on the attributes of the current mode is true. If our system is

not deterministic, we can allow multiple transitions on the same condition, and assign a probability to the occurrence of each transition (e.g. when commanded open, a closed valve usually opens but may stick closed with some probability  $p$ ). All of this information can be encoded using an automaton to represent each component. For example, a valve might be represented as shown in Figure 4.

The ovals in Figure 4 represent the possible modes of the valve, *open*, *closed*, *stuck open* and *stuck closed*. Each mode includes a partial description of how the valve behaves in that mode. For example, when the valve is in the closed mode, the flow through the valve is zero. The arcs specify how the mode changes when an action is taken. Starting in the closed mode, when the command to open is given, the most likely outcome is that the valve moves to the open mode via the darker arc. The lighter arcs represent less likely failure transitions to the stuck open or stuck closed mode that may occur.

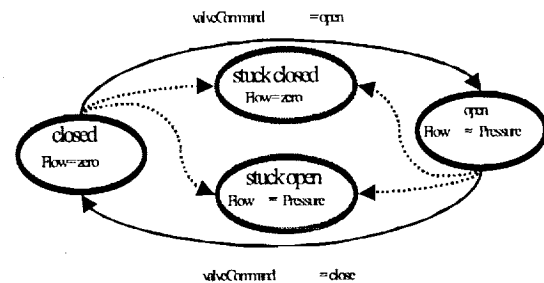


Figure 4 - Valve Automaton

Using a single component, we can develop a basic intuition for how a discrete control algorithm might work. For the sake of simplicity, the algorithm is broken down into a method for estimating the state of the system given the sensors and a method for determining the best action to take given the state estimate. Suppose we know a valve to be in the closed mode, and we issue the command to open the valve. We then receive an observation of the flow and pressure, and wish to determine the new state of the valve. Suppose the flow reported by the sensor is zero and the pressure is high. We investigate each possible transition from the closed mode in turn. If the valve took the likely transition to the open mode, the flow through the valve would be proportional to the pressure. It is not, so this transition, although likely, is ruled out. Similarly, the less likely transition to the stuck open mode is ruled out by the observations. The only transition consistent with the observations is the

stuck closed mode, and this becomes our state estimate. The basic intuition is that *diagnosis is a search over the transitions of the hardware model to find a mode that is consistent with the observations.*

Choice of a control action is accomplished in a similar manner. Suppose we again know the valve to be in the closed mode. We wish to have flow through the valve. We first check to see if the current mode allows flow. It does not, so we must find a path to a mode that does. We cannot use any of the arcs to failure modes in our path, as we cannot force failures to occur. Instead, we must use only the commandable (darker) arcs. In this case, there is only one arc from the closed mode to the open mode. Fortunately, in the open mode there must be flow and our search ends. The basic intuition is that *action selection is a search over the transitions of the hardware model to find a mode that enforces the desired conditions.*

The search for a diagnosis or control action naturally extends to multiple components. Consider the simplified propulsion system of Figure 5. Consider the case where we have commanded all three valves  $V_1$ ,  $V_2$  and  $V_3$  to open. From the interconnections of the components, we can automatically infer that the pressure in the He tank is pressurizing the input of  $V_3$ . From the valve model, we can predict there is a pressure and flow through  $V_3$ . Similarly, we predict that the  $O_2$  and fuel tanks are pressurized, and there is a flow of  $O_2$  and fuel to the engine through  $V_1$  and  $V_2$ . From the engine model, we predict acceleration given the flow of oxidizer and fuel. If no acceleration is measured, the assumption that the system is operating properly is inconsistent, and a search for a consistent set of mode transitions is required. Conceptually, this is a search over all of the components to find a set of failures that are consistent with the current observations.

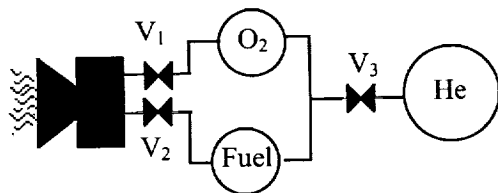


Figure 5 A Simplified Propulsion System

In practice, considering every possible combination of component failures would be expensive and unnecessary. Using observations, we can quickly focus the search to the relevant components. For example, a flow at  $V_1$  was previously predicted because of the assumed states of  $V_1$ , the  $O_2$  tank,  $V_3$

and the He tank. If we measure no flow at  $V_1$ , then at least one of these components must have suffered a failure. Similarly, if we measure a pressure at  $V_2$ , then it is inconsistent to believe the He tank is ruptured or  $V_3$  is stuck closed. Thus with two observations we have focused our search for a diagnosis on  $V_1$  and the  $O_2$  tank. We may then consider possible failures of  $V_1$  or the tank in turn, and check if the model of each failure mode is consistent with the observations. In larger systems, the focusing effect of observations can be even greater. For example, in the propulsion system of Figure 3, observation of pressure at the oxidizer tank removes all fourteen components to the right of the observation from consideration in the diagnosis. For a more detailed account of these techniques, please see (Williams & Nayak, 1996; Kurien & Nayak, 2000).

We have successfully applied these discrete diagnosis and control techniques to a number of domains. Models of the propulsion systems of the Cassini spacecraft (Pell, et al, 1996) and X-34 vehicle as well as subsystems of the X-37 spacecraft have been developed and tested in simulation. A model of the reaction control, power and other systems of the Deep Space 1 spacecraft was tested in flight (Bernard, et al, 1998). In the next section, we describe a seemingly similar domain in which our attempts to apply discrete diagnosis and control techniques were not as straightforward.

#### 4 Reverse Water Gas Shift

In-Situ Resource Utilization has become a key component of NASA's plans for Mars exploration. Major cost savings are possible when propellants and other consumables are manufactured on Mars instead of being imported from earth. The reverse water gas shift reaction (RWGS) is a chemical reaction that produces oxygen ( $O_2$ ) from the atmosphere of Mars, which is mostly carbon dioxide ( $CO_2$ ).

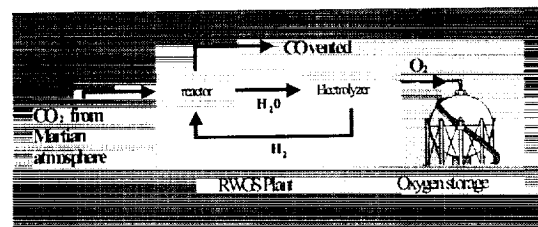
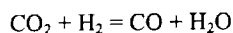


Figure 7 – RWGS Plant on Mars

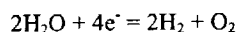
The RWGS reaction occurs when  $CO_2$  is combined with hydrogen ( $H_2$ ) as shown in Equation 1. The water produced is electrolyzed (Equation 2) the oxygen from

electrolysis is stored, and the H<sub>2</sub> is recirculated into the input stream (see Figure 7).

#### Equation 1



#### Equation 2



#### Equation 3

$$\text{CO} = \text{minimum}(\text{H}_2, \text{CO}_2)$$

Since all the H<sub>2</sub> is reused, only a small amount needs to be imported from earth. The net result of the RWGS plant is to produce as much O<sub>2</sub> as needed for propellant or life support using only CO<sub>2</sub> from the Martian atmosphere as a raw material.

As a byproduct of the reaction of Equation 1, The RWGS reactor vents carbon monoxide (CO). When two reactants are supplied in the correct ratio both are completely converted into products with no excess of either left over. If the molar ratio of feed gases in RWGS is not exactly 1:1, excess H<sub>2</sub> or CO<sub>2</sub> will also vent. Equation 3 expresses this constraint. The control challenge is to supply CO<sub>2</sub> and H<sub>2</sub> to the reactor in exactly the right amounts to maximize production and avoid wasting either gas - particularly H<sub>2</sub> that is relatively scarce on Mars. Among other things, the plant control system must monitor the vent stream, detect if either feed gas is in excess and adjust flows to continue efficient operation. RWGS must operate for several years on Mars without human intervention, so its control system must be autonomous and highly reliable. One of the most common fault modes for process equipment in harsh environments is instrumentation failure. One or more measurements may prove defective over the operating lifetime of the system. However, given the remaining sensors and knowledge of the RWGS process, it is possible for a control system to continue producing O<sub>2</sub> without intervention from ground controllers. The control system must infer the missing instrumentation data and correctly select control actions.

The RWGS plant can be viewed as a constraint network (see Figure 9 below). There are eleven parameters constrained by four real-valued functions (F1, F2, F3 & F4). Five of the parameters are monitored by measurements from the plant, and two others are commands used to control the system. The constraint network of Figure 9 may be used for both automated diagnosis and control. Conceptually, this could be accomplished in a manner similar to that described in the previous section. To perform

diagnosis, when one or more measurements from the plant is inconsistent with values predicted by the constraint network, we could attempt to isolate the fault by suspending one constraint at a time and calculating a value for it using the others. If the new value can be computed consistently, the suspended constraint is a valid fault suspect. To perform reconfiguration or more general control, we could express an operating goal as a set of constraints and attempt to invert the constraint network to calculate the commands that will satisfy it. We attempted to build a discrete, qualitative model of the RWGS constraint network to do exactly this.

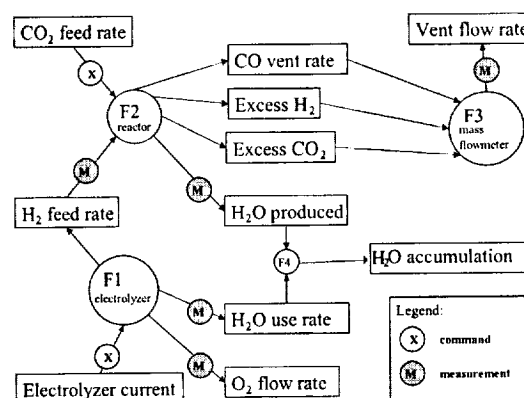


Figure 9 – Constraint network for RWGS

In order to produce a qualitative model of a continuous system, we must discretize the variables and constraints that model the system's behavior. In the thermostat example, we discretized a continuous model of the temperature change over time into a discrete model specifying whether the derivative of the temperature was positive or negative. In order to diagnose the reaction control system of Deep Space 1, we discretized the measured error between the desired and actual orientation of the spacecraft in three dimensions into three variables that captured whether the deviation on each axis was positive, negative or approximately zero. For each of these discretizations, we would write a small piece of software, referred to as a *monitor*, to convert from the real-valued sensor reading into the appropriate discrete category.

In order to develop a qualitative model of the RWGS system, we first characterized continuous variables such as electrolyzer current and H<sub>2</sub> flow rate as "low, expected or high". This allowed us to start writing

discrete constraints, for example relating the qualitative flow rate of  $H_2$  and  $CO_2$  to the qualitative rate of  $H_2O$  production. Intuitively, if the  $H_2$  input to the reaction is lower than expected, then the  $H_2O$  will be low as well. It soon became clear this qualitative abstraction of the system was inadequate. Often, a “low” value was the expected value. For example, if we intentionally turn a valve off, for example in a redundant, unused branch of the system, then the expected flow rate in the branch is zero. The sensed value zero thus corresponds the qualitative value “expected”. However, if the  $H_2O$  output of the reactor is zero, the qualitative value is “low”. We addressed this problem by quantifying flows using both the “low, expected, high” discretization and a “zero, positive” discretization and augmenting our valve, flow controller and other models to correctly predict one or both types of value. This significantly complicated the model. Unfortunately, this still was not adequate to correctly diagnose the relevant failures.

Consider the case where the current to the electrolyzer is reduced by the RWGS controller. By function F1 of the constraint diagram, the  $H_2$  feed rate will be correspondingly reduced according to some continuous function. However, this is as expected. That is to say, we do not need to diagnose a failure to explain the reduced rate. In order to accommodate this in a qualitative model that cannot perform continuous calculations, it became necessary to compute such relationships between variables *outside* of the model. This made it possible to relate “expected” electrolyzer current to “expected”  $H_2$  flow by a continuous function. Whatever operating level was required for the electrolyzer, the external function would compute the “expected”  $H_2$  flow that could be compared to the observed values in order to report “low, expected or high”. We could then perform a system-wide, discrete diagnosis. This arrangement is awkward and requires maintenance of separate auxiliary code. Other variables in RWGS required comparisons between two or more quantitative values; these relationships were almost impossible to model qualitatively. In particular, the reactor function F2 is a comparison between two real-valued parameters,  $H_2$  flow and  $CO_2$  flow (Equation 3) that we could not adequately capture within the discrete model.

In retrospect, the Cassini propulsion system model is something of a special case. At the level of detail to which it was modeled, it consists of a pressurized tank at one end and vacuum at the other. The control flow and pressure gradient in this system are always in one

direction. There are no closed loops or mixing of flows. The diagnosis problem was only concerned with abrupt failures such as stuck valves, and did not attempt to capture leaks, flow reversions, or more subtle flow anomalies. No diagnosis required observing the system over time. Thus, we could perform our diagnosis using only a context-free discretization of the observations (*e.g.*, flow, no flow). Similarly, the control problem was defined to only concern discrete actions such as opening and closing valves. There was no need to estimate and adjust continuous parameters of the system such as flow rates. In such domains, a discrete, qualitative model is often effective. In these cases, the ease of modeling and computational efficiency of a discrete, qualitative model are attractive.

In contrast, the RWGS system and many other problems involve branching or multi-directional propagation of fluid flows, electrical current or similar quantities, and capacitance, such as storage tanks or buffers, that evolves over time. Often it is extremely difficult to produce a discrete abstraction of such a domain that is both consistent with respect to diagnosis and relevant with respect to control. In the following section we provide some intuitions from the RWGS domain on where the trouble arises.

## 5 Issues with Continuous Variables

Consider again the complete constraint network for RWGS (Figure 9). Such a constraint network provides many opportunities to exploit analytical redundancy in the system measurements, and we would like to use it to devise an RWGS control system that is extremely robust and fault-tolerant. There are many other spacecraft systems that are characterized by multiple quantitative constraints in complex relationships. Below we discuss diagnosis and control problems on this network that we were unable to adequately address using a discrete model because of complex interactions of the continuous variables. For each we create a table illustrating the relevant continuous constraints that were involved, and the nature of the constraint satisfaction we were unable to perform in the discrete abstraction.

### Sensor Fault Example

Table 1 uses analytic redundancy to find a sensor failure. The columns of the table correspond to the continuous variables of the RWGS system. The rows correspond to the operation of constraints to fill in variable values. The first row specifies the constraints themselves. For clarity, only the constraints associated with the electrolyzer (function F1) are shown.

**Table 1 – Diagnosing faulty H<sub>2</sub> measurement**

Row	Electrolyzer Current amps	H <sub>2</sub> gMol/hr	H <sub>2</sub> O cc/min	O <sub>2</sub> gMol/hr	
1	I	I*0.33	I*0.10	I*0.17	Function F1
2	15	4.95	1.5	2.55	Predicted
3	15	8	1.5	2.55	Observed
4	24/15	8	1.5	2.55	Suspend amps
5	15	4.95	1.5	2.55	Suspend H <sub>2</sub>

Suspended constraint	4.95	Discrepancy	8
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**Row 1** – Functions for constraint calculations

**Row 2** – Assuming the electrolyzer current reading of 15 amps is correct, the constraint network predicts H<sub>2</sub> flow of 4.95 gram Moles per hour. The *observed* H<sub>2</sub> flow (Row 3) is 8. Thus either the current measurement or flow measurement is faulty.

**Row 4** - Suspending the current measurement, we invert the formula F1 in Row 1 and calculate current from H<sub>2</sub> (8/0.33=24 amps) H<sub>2</sub>O (1.5/0.1=15 amps) and O<sub>2</sub> (2.55/0.17=15 amps). Failure of the current measurement alone is not a consistent diagnosis.

**Row 5** – Suspending the H<sub>2</sub> constraint we calculate 4.95 for H<sub>2</sub> from electrolyzer current, H<sub>2</sub>O and O<sub>2</sub>. These results *are* consistent. Failure of the H<sub>2</sub> measurement alone is consistent.

### Control Examples

Table 3 is an example illustrating control. Suppose the goal for electrolyzer operation is O<sub>2</sub> flow of 2.0 gram moles per hour.

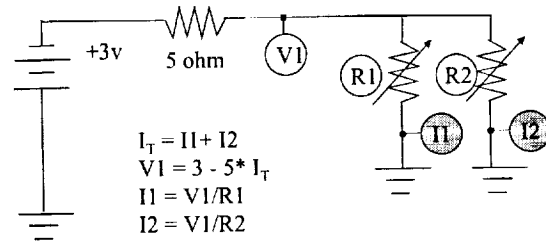
**Table 3 – Controlling O<sub>2</sub> flow**

	Electrolyzer Current amps	H <sub>2</sub> gMol/hr	H <sub>2</sub> O cc/min	O <sub>2</sub> gMol/hr	
1	I	I*0.33	I*0.10	I*0.17	Function F1
2	?	?	?	2.0	Goal for O <sub>2</sub>
3	11.76			2.0	Calc amps
4	11.76	3.9	1.2	2.0	Calc others

**Row 3** – Inverting F1, we can calculate the electrolyzer current that will yield the desired flow (2.0/0.17 = 11.76 amps).

**Row 4** – Using the value for current we can calculate expected values for H<sub>2</sub> and H<sub>2</sub>O.

The electrical circuit (Figure 10) provides another example of a system that depends on comparison between two quantitative constraints. Currents I1 and I2 depend on the resistance of R1 and R2 plus the other circuit components.



**Figure 10 – Resistor Problem**

Table 4 illustrates a control problem for this circuit. The goal is to equalize current through both resistors at 0.18 amps each. Simply increasing resistance R1 to reduce its current won't work; that would produce excess current in R2. Both resistors have to be adjusted to achieve the goal.

**Table 4 – Resistor Problem Constraint Solution**

	V1 volts	R1 ohms	R2 ohms	I1 amps	I2 amps	
1	3 - 5*I <sub>T</sub>	R1	R2	V1/R1	V1/R2	Function
2	0.35	1.00	2.00	0.35	0.18	Initial cond
3	?	?	?	0.18	0.18	Goals
4	1.2					Calculate V1
5	1.2	6.7				Calculate R1
6	1.2		6.7			Calculate R2
7	1.2	6.7	6.7	0.18	0.18	Final cond

**Row 2** – Initially, I1=0.35 amps and I2=0.18 amps

**Row 4** – To see if the goal is possible, we first must calculate V1. From the first constraint in Figure 10 we know that I<sub>T</sub> = I1+I2 (0.18 + 0.18 = 0.36 amps) The constraint in Row 1 gives us V1 = 3 - 5\*I<sub>T</sub> (3 - 5\*0.36 = 1.2 volts)

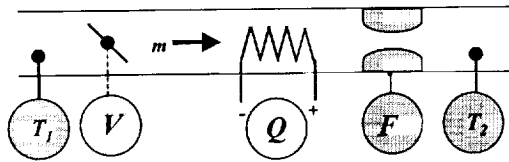
**Row 5&6** – Invert the function for I1 and solve for R1 = R2 = V1/I1 (1.2/0.18 = 6.7 ohms)

**Row 7** – Final conditions meet the control goal.

### More Complex Diagnosis and Control

Figure 11 illustrates a quantitative model characteristic of life support and various industrial systems. A fluid is flowing through a duct. The flow rate is controlled by a butterfly valve *V* and measured by a flow meter *F*. Temperature of the fluid is controlled by the heater *Q* and measured by temperature sensors *T*<sub>1</sub> and *T*<sub>2</sub>. This system can be analyzed very well with a constraint network and can be quite robust even when some of the sensors fail.

$$T_2 = \frac{Q}{mC} + T_1$$



**Figure 11 - Fluid Flow in a Duct**

Consider the failure of flow meter  $F$  that is analyzed in Table 5. In this example the fluid is water. The equation at the top of Figure 11 expresses the relationship between mass flow  $m$ , heat  $Q$  and temperatures  $T_1$  and  $T_2$ .  $C$  is the heat capacity of water – a constant equal to 1.0 cal/g. For clarity we can assume that the mass flow  $m$  is equal to the flow command  $F$ . By suspending constraints in rows 4-7 we diagnose that the flow measurement  $F$  is faulty and should be 30 instead of 2.

**Table 5 - Duct Flow Meter Failure**

	$T_1$ °C	$F$ g/hr	$Q$ cal	$T_2$ °C	
1	$T_1$	$m$	$Q$	$\frac{Q}{mC} + T_1$	Function
2	25	30	300	35	Predicted
3	25	2	300	35	Observed
4	25/-115	2	300	35	Suspend $T_1$
5	25	30	300	35	Suspend $F$
6	25	2	20/300	35	Suspend $Q$
7	25	2	300	35/175	Suspend $T_2$

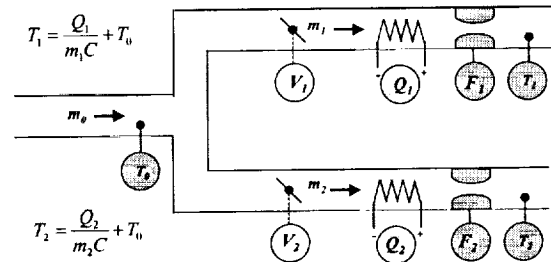
Once the flow meter is known to be faulty we can still control the duct flow by reference to the remaining measurements. (Refer to Table 6). If we want mass flow  $m$  of 40 g/hr while at the same time maintaining 35°C for  $T_2$ , we can set flow control to 40 without reference to the flow measurement and calculate a new value for  $Q$ . The proper flow and heater settings are confirmed by observing the rest of the measurements.

**Table 6 – Duct Control with Degraded Sensors**

	$T_1$ °C	$F$ g/hr	$Q$ cal	$T_2$ °C	
1	$T_1$	$m$	$Q$	$\frac{Q}{mC} + T_1$	Function
2	?	40	?	?	Goal for $m$

3	?	?	?	35	Goal for $T_2$
4		40			Calculate $F$
5	25	40	400	35	Calculate $Q$
6	25		400	35	Observed

The usefulness of quantitative constraints is more apparent when the principles illustrated by the electrical circuit and fluid flow examples are combined. Figure 12 shows two ducts connected to a common manifold. Since  $m_0 = m_1 + m_2$  if we attempt to increase flow by opening  $V_1$ ,  $m_1$  will increase; but  $m_2$  will decrease at the same time. The interconnected nature of the constraints makes for a complicated network, but there is a significant advantage in flexibility for diagnosis and control. For example, the temperature measurements may be used to confirm that duct flows are correct even if flow measurements become defective as in Table 5. Flow measurements may likewise stand in for faulty temperature sensors. Under some circumstances, it is possible to adjust flow in one duct if its control valve is inoperative by tweaking the valve in the other duct. Only if we have a model of the continuous behavior of the system will we be able to create this level of flexibility and fault tolerance.



**Figure 12 - Two-Duct Flow**

### Time-related Problems

A further example from RWGS (Figure 13) illustrates another class of problems that is difficult to manage using a discrete model. In this case, the issue is the discrete, non-metric model of time. Suppose we wish to fill the tank. Knowing the initial water level in the tank  $LL_0$  it is possible to predict what the liquid level measurement will read at some arbitrary time  $t$ . With a predicted level, one can continuously monitor the system and diagnose a faulty level sensor  $LL$ , flow meter  $F$  or broken pump as soon as the measured level deviates from the prediction. With a discrete time and discrete state model, one simply cannot represent the evolution of the water level over time. Our experience



has been this makes representation of systems with capacitance of any kind very difficult to represent.

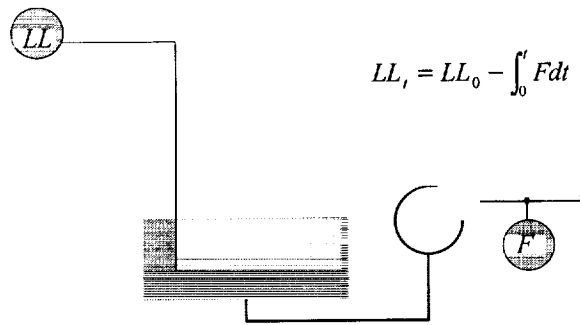


Figure 13 - Tank Level Problem

## 6 Conclusions

We have provided a succinct conceptual introduction to hybrid, continuous and discrete systems and explored the primary concepts behind model-based, discrete diagnosis and control in a manner we hope is accessible to those outside the field. We have found that discrete models, in particular for model-based diagnosis and control, can be quite attractive. For appropriate domains, they are intuitive, simple to encode, and computationally tractable. We have given an example of a domain where discrete models and techniques were quite useful, and attempted to characterize it. In particular, a discrete abstraction is useful where the abstraction of each variable from a continuous-valued variable to a discrete variable can be performed independent of other variables and the particular configuration of the system being modeled. In addition, there are many applications that require hybrid models with both discrete and continuous components. We have provided an example of such a domain, and attempted to illustrate some of its characteristics. In particular, hybrid models are essential where the physical system is characterized by continuous variables whose discrete characterization is dependent upon some context, that are summed or multiplied, that branch in multiple directions or that are compared to each other. Our experience with the RWGS system suggests that making use of a hybrid representation would present many opportunities to build systems that are very robust and fault-tolerant – able to operate with missing information and helping solve control problems that will enable future planetary exploration.

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